# ECE 204 Introduction to Digital Logic Bill Nelson Homework \#7 

NAME: $\qquad$ Due: 03/06/2017

Show your work. Answers without supporting work will not earn full credit. Ignore all flip-flop sets and resets.

1. Draw a five $D$ flip-flop Johnson counter. Do not include forbidden state detection. Assuming the flip-flops are initially all ones, show the successive states through the return to all ones.

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2. Given the following circuit, generate its state chart and draw its state diagram.


| $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{A}$ | $\mathbf{X}^{+}$ | $\mathbf{Y}^{+}$ | $\mathbf{Z}$ | $\mathbf{D}_{\mathbf{X}}$ | $\mathbf{D}_{\mathbf{Y}}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 |  |  |  |  |  |
| 0 | 0 | 1 |  |  |  |  |  |
| 0 | 1 | 0 |  |  |  |  |  |
| 0 | 1 | 1 |  |  |  |  |  |
| 1 | 0 | 0 |  |  |  |  |  |
| 1 | 0 | 1 |  |  |  |  |  |
| 1 | 1 | 0 |  |  |  |  |  |
| 1 | 1 | 1 |  |  |  |  |  |

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PROBLEM \#2, Continued:


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3. Given the following state diagram, generate the corresponding state chart including the D inputs. Also give the minimized equations for the $\mathbf{D}$ inputs and for the output, $\mathbf{B}$. Let the state bits be labeled $\mathbf{X}$ and $\mathbf{Y}$, the input $\mathbf{A}$ and the output $\mathbf{B}$.


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PROBLEM \#3, Continued:

| $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{A}$ | $\mathbf{X}^{+}$ | $\mathbf{Y}^{+}$ | $\mathbf{B}$ | $\mathbf{D}_{\mathbf{X}}$ | $\mathbf{D}_{\mathbf{Y}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 |  |  |  |  |  |
| 0 | 0 | 1 |  |  |  |  |  |
| 0 | 1 | 0 |  |  |  |  |  |
| 0 | 1 | 1 |  |  |  |  |  |
| 1 | 0 | 0 |  |  |  |  |  |
| 1 | 0 | 1 |  |  |  |  |  |
| 1 | 1 | 0 |  |  |  |  |  |
| 1 | 1 | 1 |  |  |  |  |  |


| $X / Y A$ | 00 | 01 | 11 | 10 |
| :---: | :--- | :--- | :--- | :--- |
| 0 |  |  |  |  |
| 1 |  |  |  |  |


| $X / Y A$ | 00 | 01 | 11 | 10 |
| :---: | :--- | :--- | :--- | :--- |
| 0 |  |  |  |  |
| 1 |  |  |  |  |


| $\mathrm{X} / \mathrm{YA}$ | 00 | 01 | 11 | 10 |
| :---: | :--- | :--- | :--- | :--- |
| 0 |  |  |  |  |
| 1 |  |  |  |  |

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4. Complete the following partial state chart by showing the necessary $\boldsymbol{J}$ and $\boldsymbol{K}$ inputs for the flip flops. Give the minimized equations for the $\boldsymbol{J}$ and $\boldsymbol{K}$ inputs and for the output, and draw the state diagram. The state bits are $\mathbf{A}$ and $\mathbf{B}$, the input is $\mathbf{C}$ and the output is $\mathbf{Z}$.

| $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{C}$ | $\mathbf{A}^{+}$ | $\mathbf{B}^{+}$ | $\mathbf{Z}$ | $\mathrm{J}_{\mathrm{A}}$ | $\mathrm{K}_{\mathrm{A}}$ | $\mathrm{J}_{\mathrm{B}}$ | $\mathrm{K}_{\mathbf{B}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 1 | 0 |  |  |  |  |
| 0 | 0 | 1 | 1 | 0 | 1 |  |  |  |  |
| 0 | 1 | 0 | 0 | 0 | 0 |  |  |  |  |
| 0 | 1 | 1 | 1 | 1 | 1 |  |  |  |  |
| 1 | 0 | 0 | 0 | 0 | 0 |  |  |  |  |
| 1 | 0 | 1 | 1 | 1 | 1 |  |  |  |  |
| 1 | 1 | 0 | 1 | 0 | 0 |  |  |  |  |
| 1 | 1 | 1 | 0 | 1 | 1 |  |  |  |  |

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PROBLEM \#4, Continued:

| A / B C | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 0 |  |  |  |  |
| 1 |  |  |  |  |


| A / B C | 00 | 01 | 11 | 10 |
| :---: | :--- | :--- | :--- | :--- |
| 0 |  |  |  |  |
| 1 |  |  |  |  |


| A / B C | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 0 |  |  |  |  |
| 1 |  |  |  |  |


| A / B C | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 0 |  |  |  |  |
| 1 |  |  |  |  |


| A / B C | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 0 |  |  |  |  |
| 1 |  |  |  |  |

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PROBLEM \#4, Continued:


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5. Given the following state diagram, generate the corresponding state chart including the necessary $\boldsymbol{J}$ and $\boldsymbol{K}$ inputs. Also give the minimized equations for the $\boldsymbol{J}$ and $\boldsymbol{K}$ inputs and for the output. Let the state bits be labeled $\mathbf{X}, \mathbf{Y}$ and $\mathbf{Z}$, the input $\mathbf{A}$ and the output $f$.


States 100, 110 \& 111 are unused. If entered, these state return to state 0XX

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PROBLEM \#5, Continued:

| $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{Z}$ | $\mathbf{A}$ | $\mathbf{X}^{+}$ | $\mathbf{Y}^{+}$ | $\mathbf{Z}^{+}$ | $f$ | $\mathrm{~J}_{\mathrm{X}}$ | $\mathrm{K}_{\mathrm{X}}$ | $\mathrm{J}_{\mathrm{Y}}$ | $\mathrm{K}_{\mathrm{Y}}$ | $\mathrm{J}_{\mathbf{Z}}$ | $\mathrm{K}_{\mathbf{Z}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 |  |  |  |  |  |  |  |  |  |  |
| 0 | 0 | 0 | 1 |  |  |  |  |  |  |  |  |  |  |
| 0 | 0 | 1 | 0 |  |  |  |  |  |  |  |  |  |  |
| 0 | 0 | 1 | 1 |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0 | 0 |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0 | 1 |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 1 | 0 |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 1 | 1 |  |  |  |  |  |  |  |  |  |  |
| 1 | 0 | 0 | 0 |  |  |  |  |  |  |  |  |  |  |
| 1 | 0 | 0 | 1 |  |  |  |  |  |  |  |  |  |  |
| 1 | 0 | 1 | 0 |  |  |  |  |  |  |  |  |  |  |
| 1 | 0 | 1 | 1 |  |  |  |  |  |  |  |  |  |  |
| 1 | 1 | 0 | 0 |  |  |  |  |  |  |  |  |  |  |
| 1 | 1 | 0 | 1 |  |  |  |  |  |  |  |  |  |  |
| 1 | 1 | 1 | 0 |  |  |  |  |  |  |  |  |  |  |
| 1 | 1 | 1 | 1 |  |  |  |  |  |  |  |  |  |  |


| $\mathrm{XY} / \mathrm{ZA}$ | 00 | 01 | 11 | 10 |
| :---: | :--- | :--- | :--- | :--- |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |


| $X Y / Z A$ | 00 | 01 | 11 | 10 |
| :---: | :--- | :--- | :--- | :--- |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |

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PROBLEM \#5, Continued:

| $X Y / Z A$ | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |


| $X Y / Z A$ | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |


| $X Y / Z A$ | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |


| $X Y / Z A$ | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |


| $X Y / Z A$ | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |

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6. Design an 8 -state state machine counter with the following characteristics:

- If the $\mathbf{e}$ (even) input is 1 , the next state is the next even numbered state (modulo 8).
- If the $\mathbf{e}$ input is 0 , the next state is the next odd numbered state (modulo 8).
- States are encoded using J-K flip-flops labeled $\mathbf{X}, \mathbf{Y} \& \mathbf{Z}$ with $\mathbf{X}$ the MSB.
- The counter has no output other than the state flip-flops. Give the state table, the state diagram and the minimized equations For the J and K inputs to each flip-flop.

| $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{Z}$ | $\mathbf{e}$ | $\mathbf{X}^{+}$ | $\mathbf{Y}^{+}$ | $\mathbf{Z}^{+}$ | $\mathbf{J}_{\mathbf{X}}$ | $\mathbf{K}_{\mathbf{X}}$ | $\mathbf{J}_{\mathbf{Y}}$ | $\mathbf{K}_{\mathbf{Y}}$ | $\mathbf{J}_{\mathbf{Z}}$ | $\mathbf{K}_{\mathbf{Z}}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 |  |  |  |  |  |  |  |  |  |
| 0 | 0 | 0 | 1 |  |  |  |  |  |  |  |  |  |
| 0 | 0 | 1 | 0 |  |  |  |  |  |  |  |  |  |
| 0 | 0 | 1 | 1 |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0 | 0 |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 0 | 1 |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 1 | 0 |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 1 | 1 |  |  |  |  |  |  |  |  |  |
| 1 | 0 | 0 | 0 |  |  |  |  |  |  |  |  |  |
| 1 | 0 | 0 | 1 |  |  |  |  |  |  |  |  |  |
| 1 | 0 | 1 | 0 |  |  |  |  |  |  |  |  |  |
| 1 | 0 | 1 | 1 |  |  |  |  |  |  |  |  |  |
| 1 | 1 | 0 | 0 |  |  |  |  |  |  |  |  |  |
| 1 | 1 | 0 | 1 |  |  |  |  |  |  |  |  |  |
| 1 | 1 | 1 | 0 |  |  |  |  |  |  |  |  |  |
| 1 | 1 | 1 | 1 |  |  |  |  |  |  |  |  |  |

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PROBLEM \#6, Continued:


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PROBLEM \#6, Continued:

| $X Y / Z e$ | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |


| $X Y / \mathrm{Ze}$ | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |


| $X Y / Z e$ | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |


| $X Y / Z e$ | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |


| $X Y /$ Ze | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |


| $\mathrm{XY} / \mathrm{Ze}$ | 00 | 01 | 11 | 10 |
| :---: | :---: | :---: | :---: | :---: |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |

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 Homework \#77. Draw a five D flip-flop PN counter using an XOR and taps at stages

3 and 5. Do not include forbidden state detection. Show the first 12 successive states assuming the initial state is $\{1,0,0,0,1\}$.

